

Machine learning and feature selection in bioinformatics

Jean-Philippe Vert

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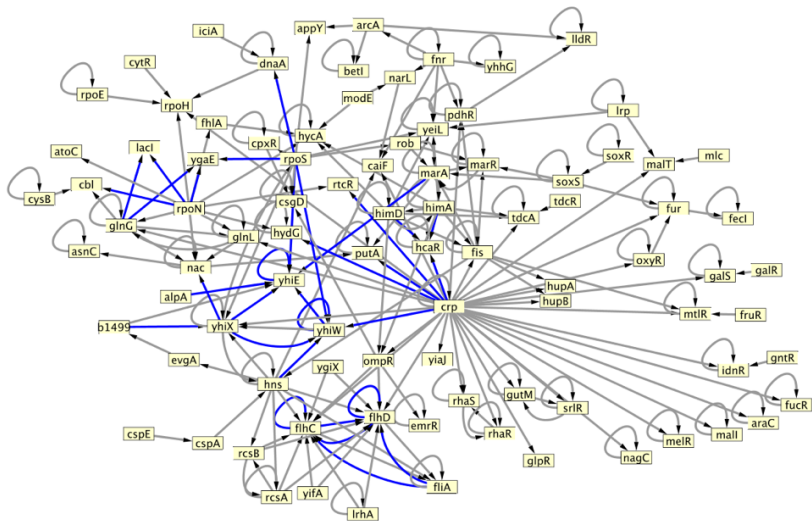
Mines ParisTech / Curie Institute / Inserm

Machine Learning for Neuroimaging workshop,
Marseille, Nov 8-9, 2011.

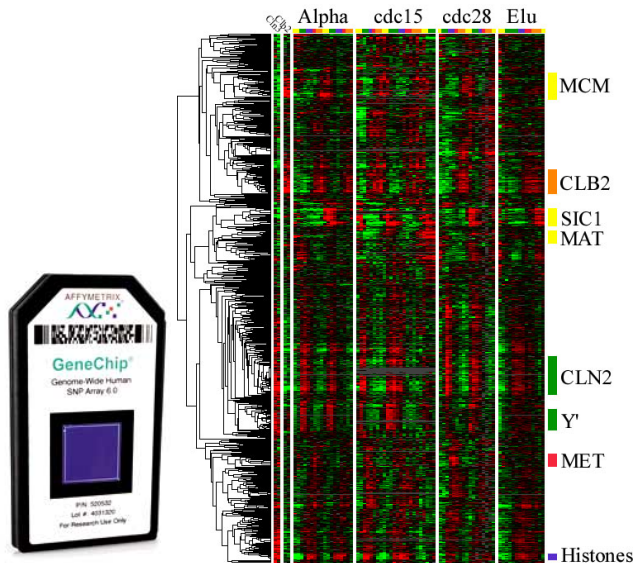
- 1 Inference of gene regulatory networks
- 2 Diagnosis and prognosis from gene expression data

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Gene regulatory network (GRN) of *E. coli*

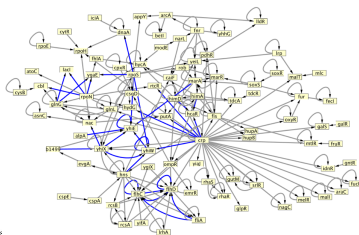
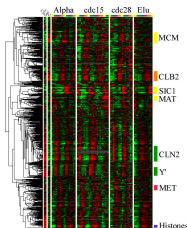


Gene expression data



GRN inference (*de novo*)

Given a set of gene expressions, infer the regulations.

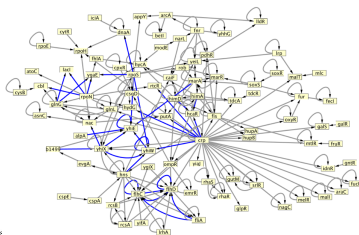
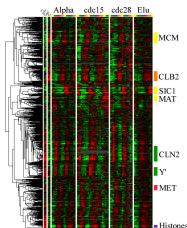


How?

- Model-based (dynamic systems)
- (Dynamic) Bayesian networks
- Similarity-based
- Feature selection

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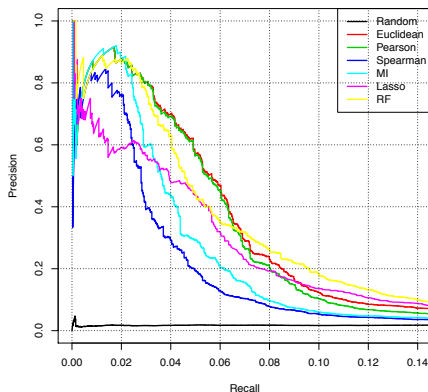
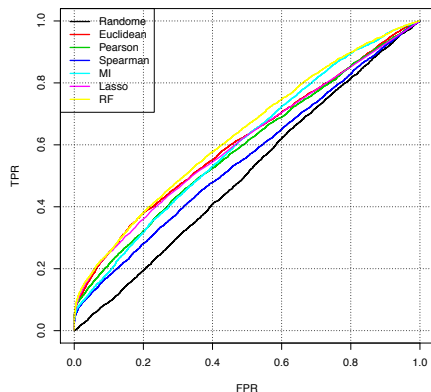
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Evaluation (DREAM challenge)

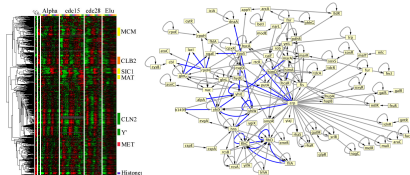


- **Best results obtained by feature selection methods**
- Bootstrap-based methods (RF, stability selection)
- Overall performance very disappointing (difficult problem...)

Supervised inference

The problem

Given a set of gene expressions AND a set of known regulations, infer missing regulations.



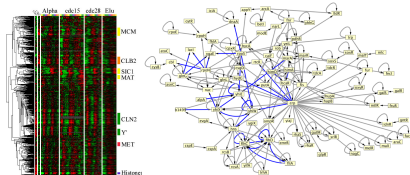
How?

- **Local models:** for each TF, learn to discriminate the regulated vs non-regulated genes
- **Global models:** learn to discriminate connected vs non-connected TF-target pairs

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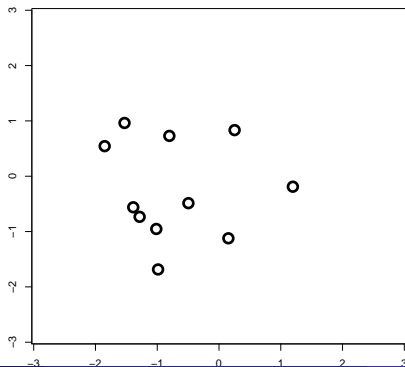


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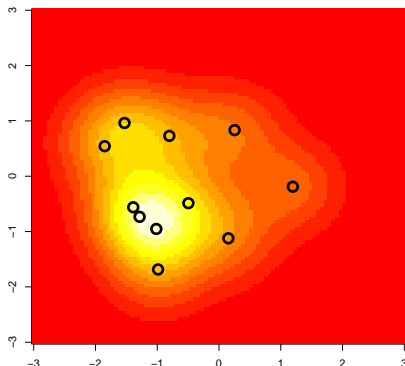
Example: one-class learning approach for local model

- For a given TF, let $P \subset [1, n]$ be the set of genes known to be regulated by it
- From the expression profiles $(X_i)_{i \in P}$, estimate a score $s(X)$ to assess which expression profiles X are similar
- Then classify the genes not in P by decreasing score



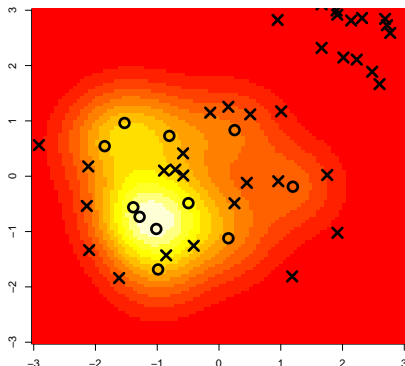
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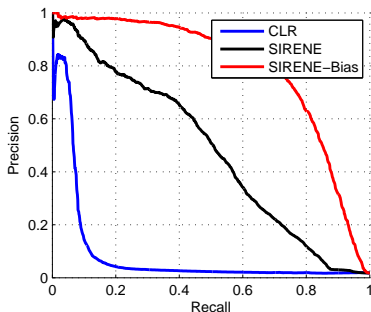
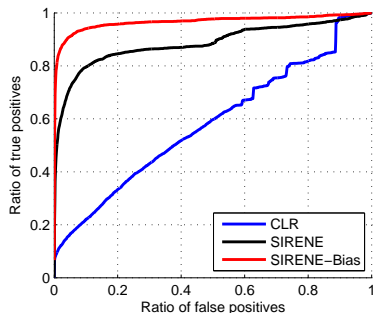


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Validation

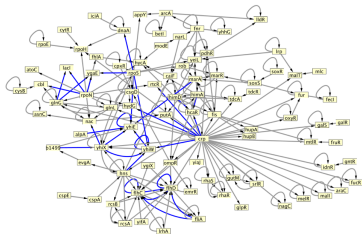


Method	Recall at 60%	Recall at 80%
SIRENE	44.5%	17.6%
CLR	7.5%	5.5%
Relevance networks	4.7%	3.3%
ARACNe	1%	0%
Bayesian network	1%	0%

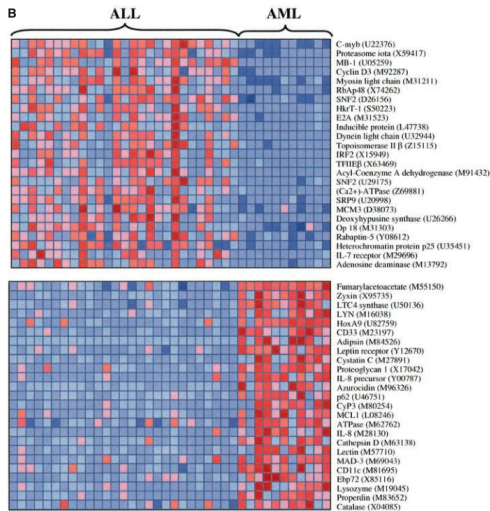
SIRENE = Supervised Inference of REgulatory Networks (Mordelet and V., 2008)

Lessons learned

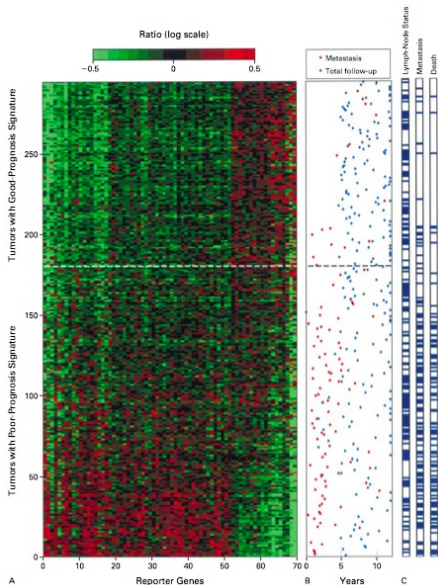
- Many ways to formalize the GRN inference problem (structure learning)
- De novo inference is best solved by **feature selection**
- **Supervised inference** better when the structure is partially known
- Simple local models outperform structured output learning
- Performance remains low. Still an open problem!



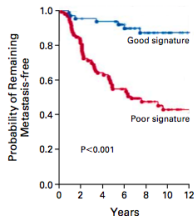
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Prognosis



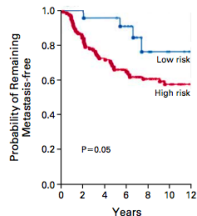
A Gene-Expression Profiling



NO. AT RISK

Good signature	60	57	54	45	31	22	12
Poor signature	91	72	55	41	26	17	9

B St. Gallen Criteria



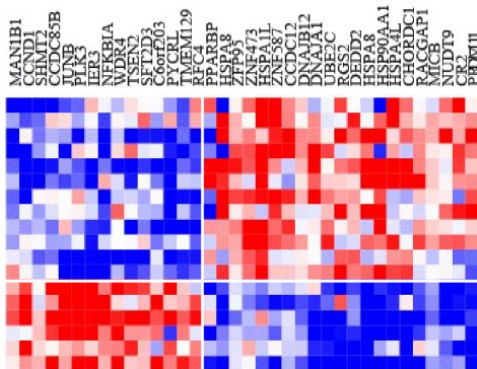
NO. AT RISK

Low risk	22	22	21	17	9	5	2
High risk	129	107	88	69	48	34	19

Gene selection, molecular signature

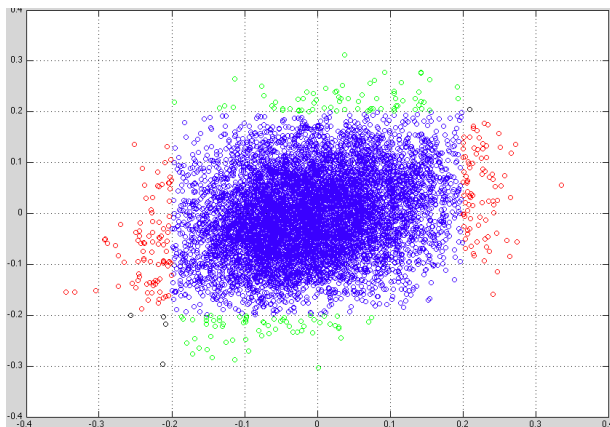
The idea

- We look for a **limited set** of genes that are sufficient for prediction.
- Selected genes should inform us about the underlying biology

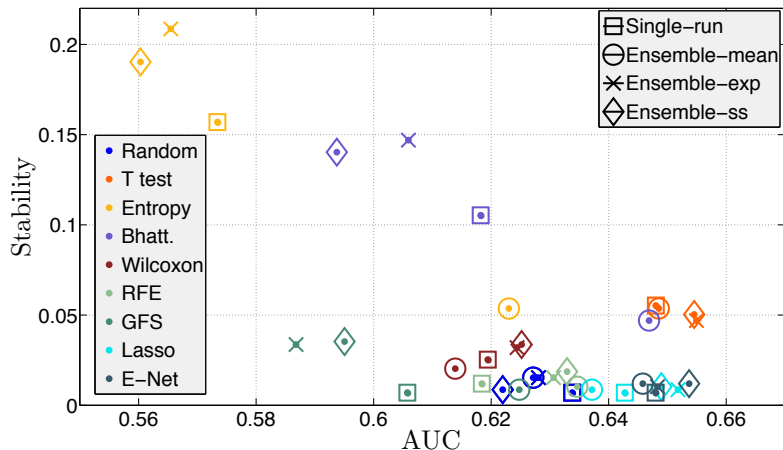


But... instability of molecular signatures

- Wang dataset: $n = 286$, $p = 8141$
- Pearson correlation with the output on 2 random subsamples of 143 samples:

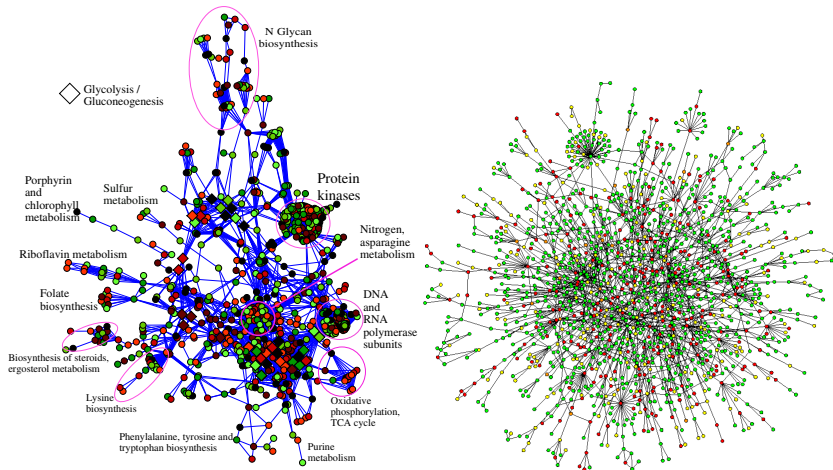


Comparison of feature selection methods...



Haury et al. (2011)

Gene networks



Motivation

- Basic biological functions usually involve the **coordinated action of several proteins**:
 - Formation of **protein complexes**
 - Activation of metabolic, signalling or regulatory **pathways**
- We know these groups through functional groups and protein networks

Shrinkage estimators with prior knowledge

$$\min_{\beta} R(\beta) + \lambda \Omega(\beta)$$

How to design penalties $\Omega(\beta)$ to encode the following hypotheses:

- 1 Connected genes on a network should have similar weights
- 2 Select few genes that are connected or belong to same predefined functional groups

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Hypothesis 1: connected genes on a network should have similar weights

- Smooth weights on the graph

$$\Omega(\beta) = \sum_{i \sim j} (\beta_i - \beta_j)^2$$

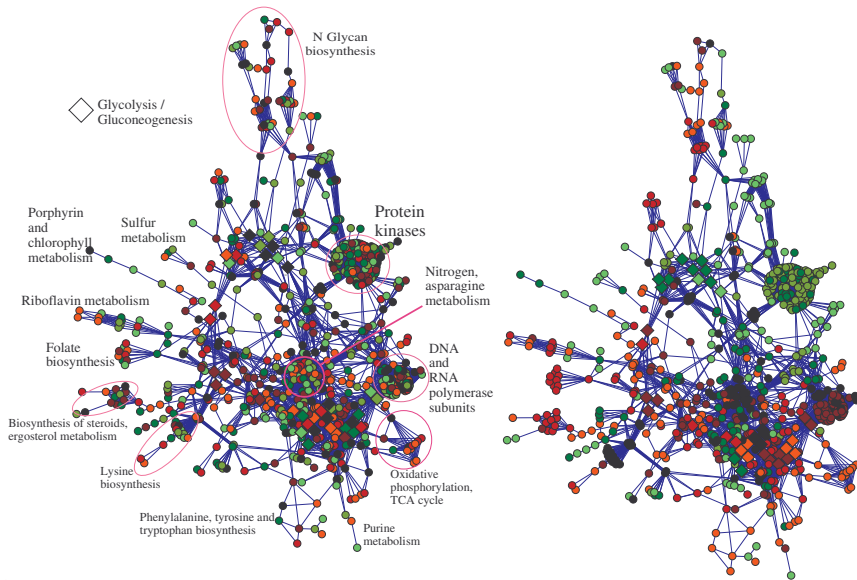
- Gene selection + smooth on the graph

$$\Omega(\beta) = \sum_{i \sim j} (\beta_i - \beta_j)^2 + \sum_{i=1}^p |\beta_i|$$

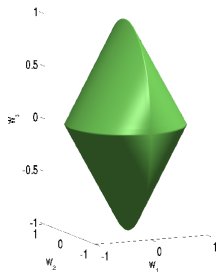
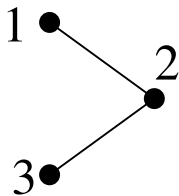
- Gene selection + Piecewise constant on the graph

$$\Omega(\beta) = \sum_{i \sim j} |\beta_i - \beta_j| + \sum_{i=1}^p |\beta_i|$$

Illustration



Hypotheses 2: select genes which are connected or belong to the same functional groups



$$\Omega(\beta) = \sup_{\alpha \in \mathbb{R}^p: \forall i \sim j, \|\alpha_i^2 + \alpha_j^2\| \leq 1} \alpha^\top \beta.$$

Graph lasso vs kernel on graph

- Graph lasso:

$$\Omega_{\text{graph lasso}}(\mathbf{w}) = \sum_{i \sim j} \sqrt{w_i^2 + w_j^2}.$$

constrains the **sparsity**, not the values

- Graph kernel

$$\Omega_{\text{graph kernel}}(\mathbf{w}) = \sum_{i \sim j} (w_i - w_j)^2.$$

constrains the values (**smoothness**), not the sparsity

Breast cancer data

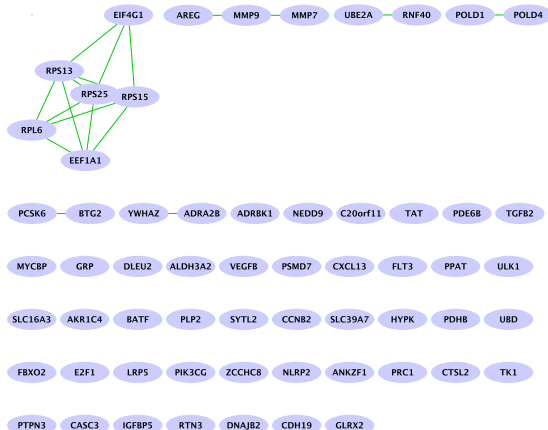
- Gene expression data for 8,141 genes in 295 breast cancer tumors.
- Canonical pathways from MSigDB containing 639 groups of genes, 637 of which involve genes from our study.

METHOD	l_1	$\Omega_{\text{OVERLAP}}^G(\cdot)$
ERROR	0.38 ± 0.04	0.36 ± 0.03
MEAN \ddagger PATH.	130	30

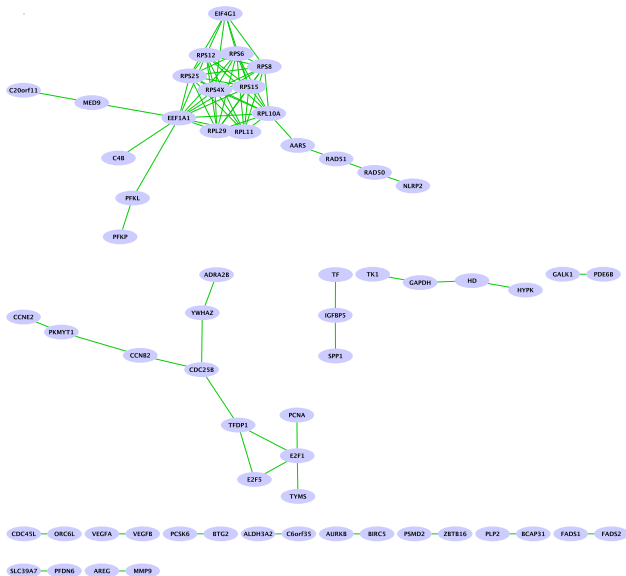
- Graph on the genes.

METHOD	l_1	$\Omega_{\text{graph}}(\cdot)$
ERROR	0.39 ± 0.04	0.36 ± 0.01
AV. SIZE C.C.	1.03	1.30

Classical lasso signature

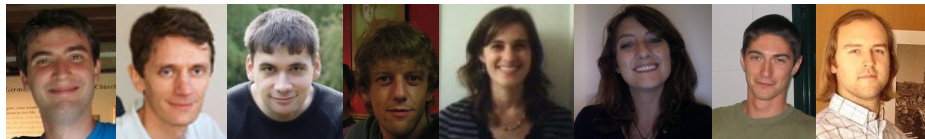


Graph Lasso signature



- **Very challenging problems**: high dimensions, few samples, complex problems (supervised classification, structure inference)
- Methods that "work" in practice find the best **trade-off** between model complexity ("bias") and ability to learn from data ("variance")
- Methods that work in theory and on toy examples do not always work on **real data** (and vice-versa)...
- Shrinkage methods for structured sparsity is promising...
- ... but difficult to reconcile **accuracy** and **interpretation**
- **Stability** may be a useful empirical proxy to assess the trust we can have in selected features

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